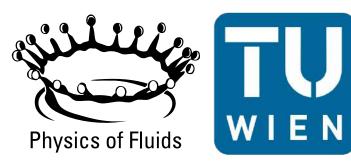


Acknowledgements



UNIVERSITY OF TWENTE.



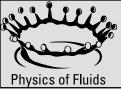


Marie Sklodowska-Curie postdoctoral fellowship No. 101062123.



Erwin Schrödinger postdoctoral fellowship No. J-4612





Acknowledgements

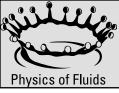


This project has received funding from the European Union's Horizon Europe research and innovation programme under the Marie Sklodowska-Curie grant agreement MEDIA No. 101062123.



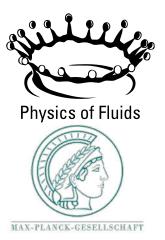


Funded by the European Union



Acknowledgements

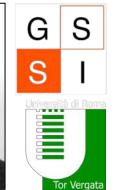
















C. Marchioli



D. Perissutti

TUWIEN



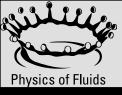








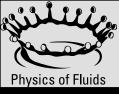
S. Pirozzoli



Presentation outline



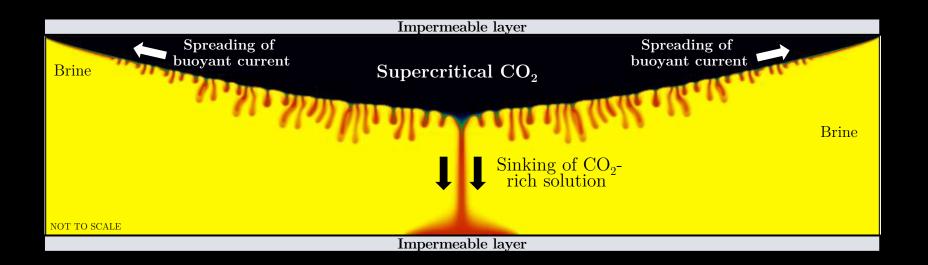
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- 4. Pore-scale modelling and dispersion
- 5. Conclusions and outlook

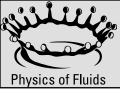


Presentation outline



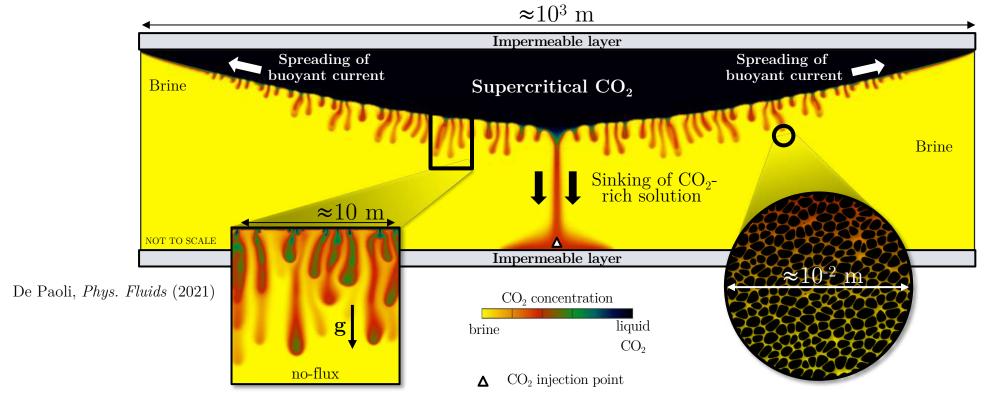
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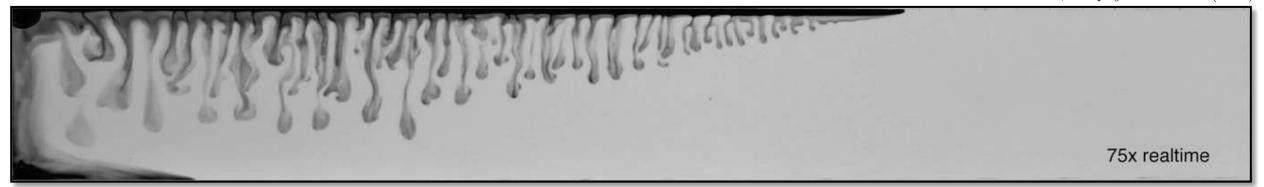


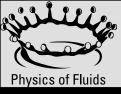
Carbon Capture and Storage





MacMinn et al., Geophys. Res. Lett. (2013)

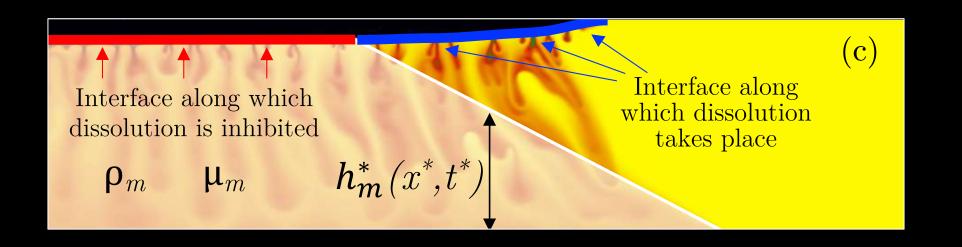


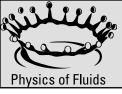


Presentation outline



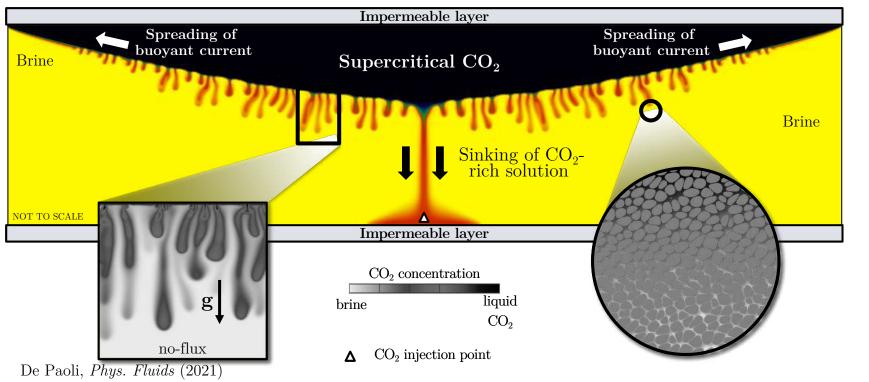
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Carbon Capture and Storage



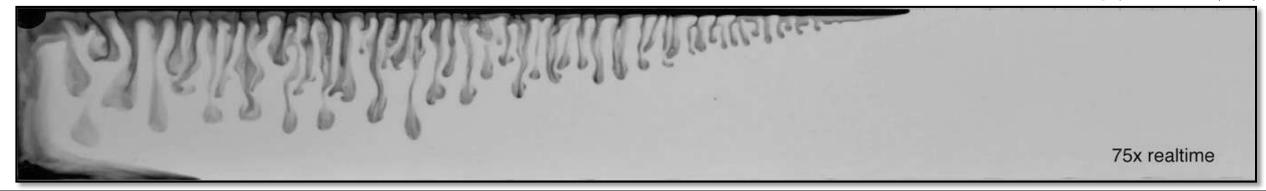


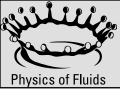
Reservoir properties

- anisotropy and heterogeneities
- finite size of confining layers
- effects of rock properties (mechanical dispersion)
- chemical dissolution and morphology variations

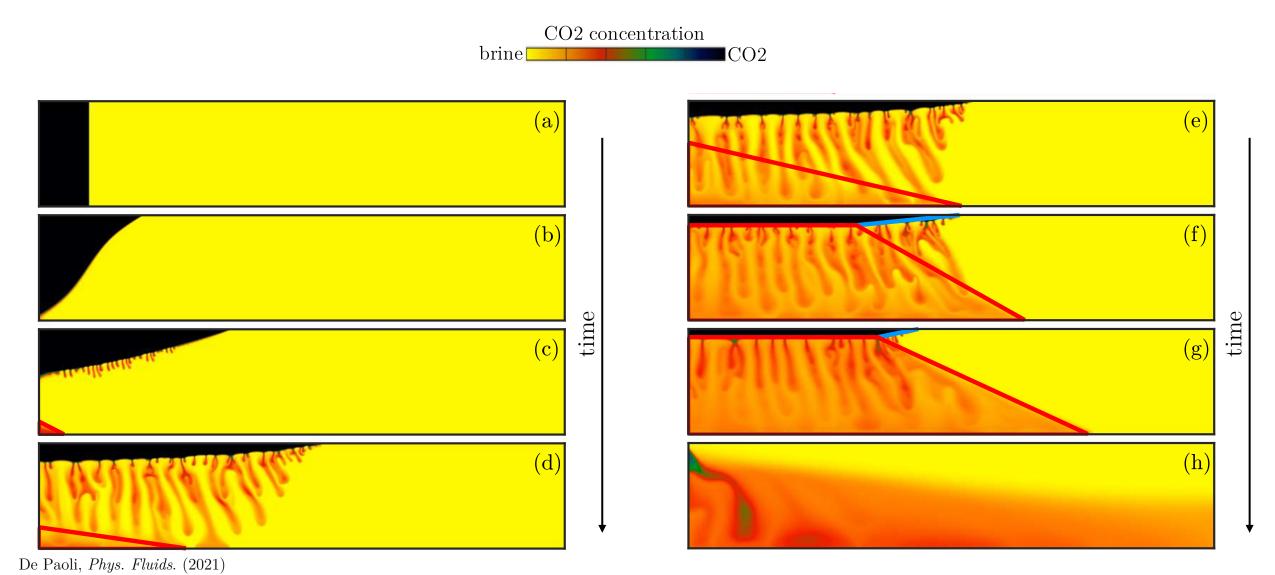
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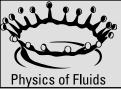
MacMinn & Juanes., Geophys. Res. Lett. (2013)



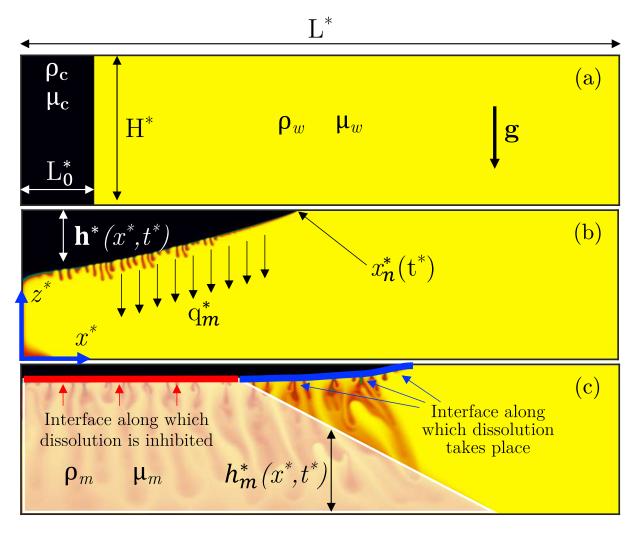










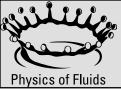


$$\nabla \cdot \mathbf{u_i^*} = 0$$

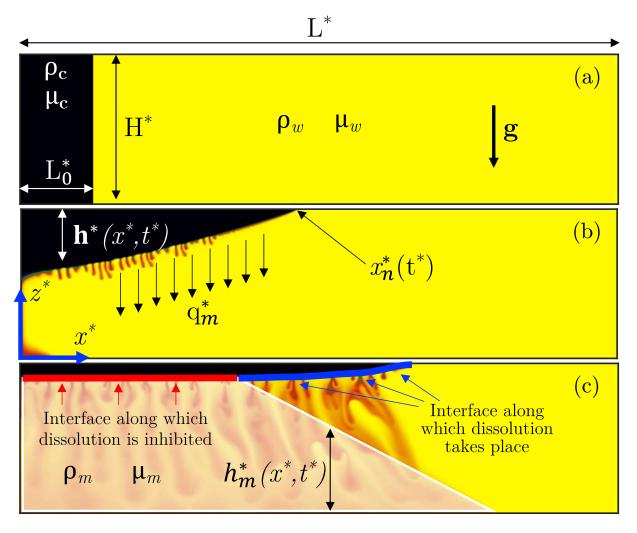
$$\mathbf{u_i^*} = \frac{1}{\mu_i} \mathbf{K} \left(-\nabla p_i^* + \rho_i \mathbf{g} \right)$$

$$\phi \frac{\partial C^*}{\partial t^*} + \mathbf{u}_i^* \cdot \nabla C^* = \phi \nabla \cdot \left[\mathbf{D}(\mathbf{u}_i^*) \cdot \nabla C^* \right]$$

De Paoli, Phys. Fluids. (2021)







$$\frac{\partial h}{\partial t} - \frac{\partial}{\partial x} \left[(1 - f)h \frac{\partial h}{\partial x} - \delta f h_m \frac{\partial h_m}{\partial x} \right] = -\varepsilon_0,$$

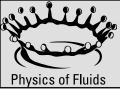
$$\frac{\partial h_m}{\partial t} - \frac{\partial}{\partial x} \left[\delta (1 - f_m)h_m \frac{\partial h_m}{\partial x} - f_m h \frac{\partial h}{\partial x} \right] = \frac{\varepsilon_0}{X_v}$$

$$f = \frac{Mh^*/H^*}{(M-1)h^*/H^* + (M_m - 1)h_m^*/H^* + 1},$$

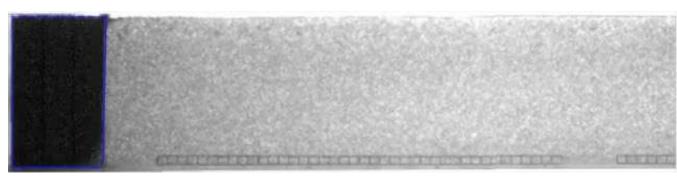
$$f_m = \frac{M_m h_m^*/H^*}{(M-1)h^*/H^* + (M_m - 1)h_m^*/H^* + 1},$$

MacMinn, Neufeld, Hesse, and Huppert, Water Resour. Res. (2012)

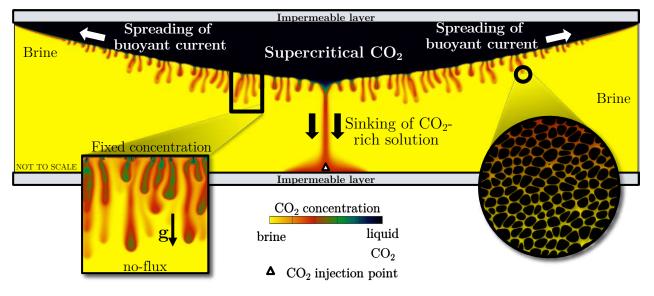
Mobility ratios
$$M = \mu_w/\mu_c$$
 and $M_m = \mu_w/\mu_m$
Buoyancy velocity ratio $\delta = W_m^*/W^*$
Volume fraction $X_v = \rho_m X_m/\rho_c$







MacMinn, Neufeld, Hesse, and Huppert, Water Resour. Res. (2012)



$$\frac{\partial h}{\partial t} - \frac{\partial}{\partial x} \left[(1 - f)h \frac{\partial h}{\partial x} - \delta f h_m \frac{\partial h_m}{\partial x} \right] = \underbrace{\left[\varepsilon_0 \right]}_{X_v}$$

$$\frac{\partial h_m}{\partial t} - \frac{\partial}{\partial x} \left[\delta (1 - f_m) h_m \frac{\partial h_m}{\partial x} - f_m h \frac{\partial h}{\partial x} \right] = \underbrace{\left[\varepsilon_0 \right]}_{X_v}$$

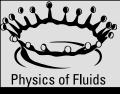
$$f = \frac{Mh^*/H^*}{(M-1)h^*/H^* + (M_m-1)h_m^*/H^* + 1},$$

$$f_m = \frac{M_m h_m^*/H^*}{(M-1)h^*/H^* + (M_m-1)h_m^*/H^* + 1},$$

$$\varepsilon_0(x) = \begin{cases}
0 & \text{if } h(x) = 0 \text{ or } h(x) + h_m(x) = 1 \\
\varepsilon & \text{else,}
\end{cases}$$

$$\varepsilon = \frac{q_m^*}{\phi W^*} \left(\frac{L_0^*}{H^*}\right)^2$$

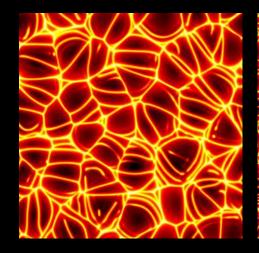
How to determine the dissolution rate q_m^* ?

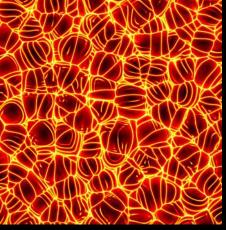


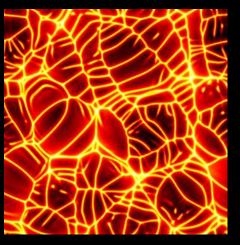
Presentation outline

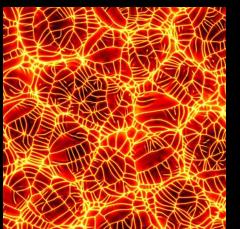


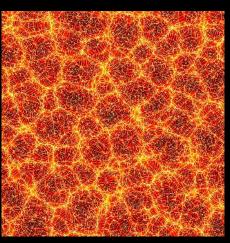
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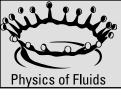












Darcy numerical simulations

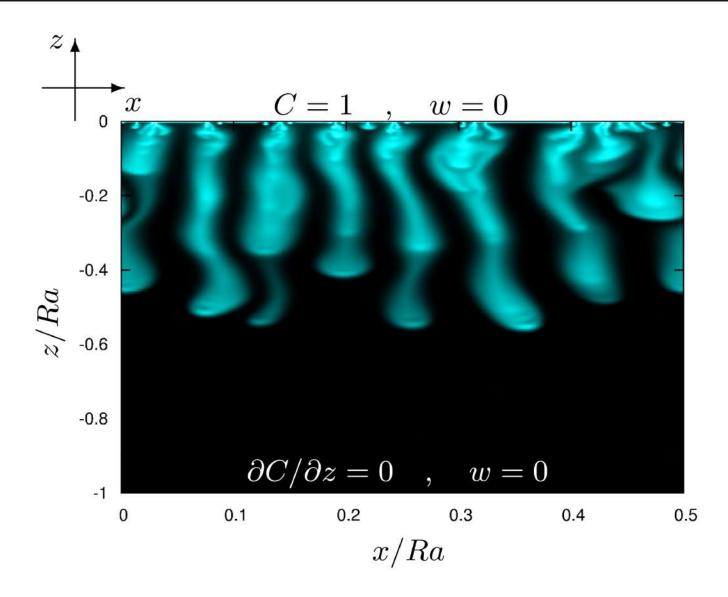


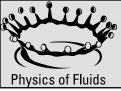
<u>Dimensionless equations</u>

$$\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} + w \frac{\partial C}{\partial z} = \frac{1}{Ra} \left(\frac{\partial^2 C}{\partial x^2} + \frac{\partial^2 C}{\partial z^2} \right)$$
$$u = -\frac{\partial P}{\partial x} \quad , \quad w = -\frac{\partial P}{\partial z} - C$$
$$\frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0$$

Governing parameter

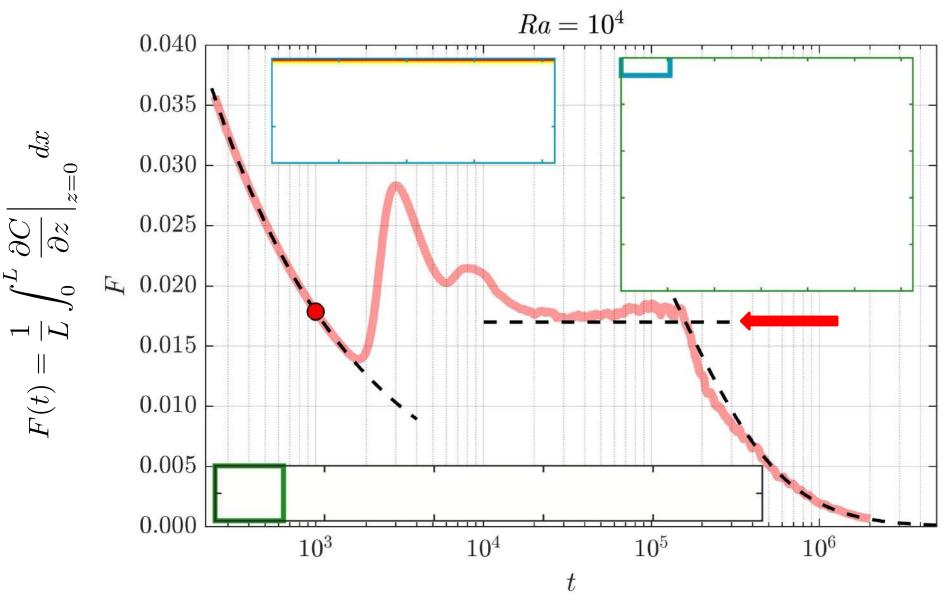
$$Ra = \frac{gH^*k_v\Delta\rho^*}{\mu\Phi D}$$



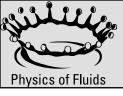


Convective dissolution process





$$Ra = \frac{gH^*k_v\Delta\rho^*}{\mu\Phi D}$$



Convection in anisotropic media



Examples of model extension: effect of **anisotropy** of the medium



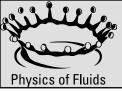
In this presentation we just consider the anisotropy of the rocks, for additional effects (lateral confinement, dispersion) see De Paoli, *Phys. Fluids* (2021)

Sedimentary rocks: Rocks formed by stratification



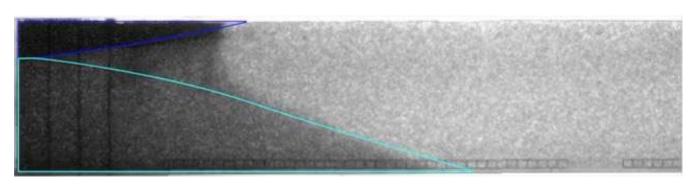
benedek / Getty Images

Rhododendrites/Wikimedia Commons/CC BY 4.0

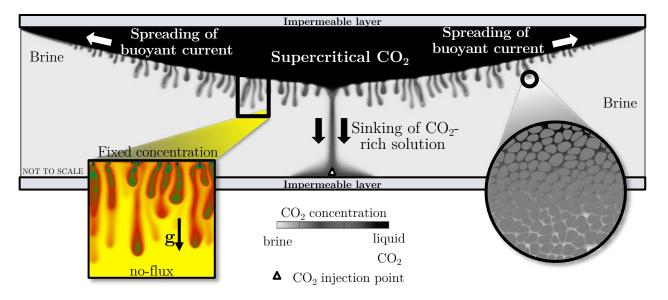


Gravity currents with dissolution





MacMinn, Neufeld, Hesse, and Huppert, Water Resour. Res. (2012)



$$\frac{\partial h}{\partial t} - \frac{\partial}{\partial x} \left[(1 - f)h \frac{\partial h}{\partial x} - \delta f h_m \frac{\partial h_m}{\partial x} \right] = \left(\varepsilon_0 \right)$$

$$\frac{\partial h_m}{\partial t} - \frac{\partial}{\partial x} \left[\delta (1 - f_m) h_m \frac{\partial h_m}{\partial x} - f_m h \frac{\partial h}{\partial x} \right] = \left(\varepsilon_0 \right)$$

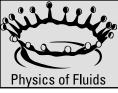
$$f = \frac{Mh^*/H^*}{(M-1)h^*/H^* + (M_m-1)h_m^*/H^* + 1},$$

$$f_m = \frac{M_m h_m^*/H^*}{(M-1)h^*/H^* + (M_m-1)h_m^*/H^* + 1},$$

$$\varepsilon_0(x) = \begin{cases}
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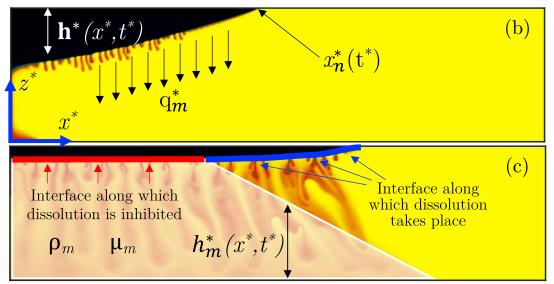
$$\varepsilon = \frac{q_m^*}{\phi W^*} \left(\frac{L_0^*}{H^*}\right)^2$$

How to determine the dissolution rate q_m^* ?

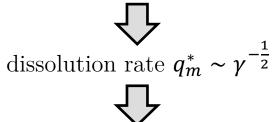


Effect of anisotropy





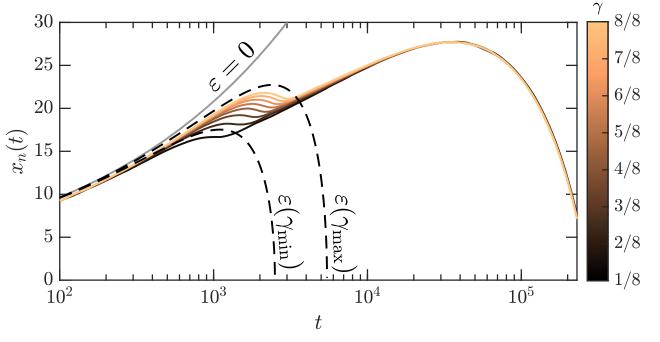
Darcy-scale simulations:



dissolution increases with the anisotropy of the medium

Sedimentary rocks are anisotropic

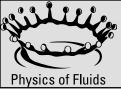
$$\gamma = \frac{k_v}{k_h} < 1$$
 $\gamma = 1$ isotropic $\gamma = 1/8$ strongly anisotropic



Analytical solution in case of

- no-dissolution ———
- independent currents ------

De Paoli, Zonta & Soldati, Phys. Fluids (2016, 2017)



Scalings of convection and finite-size effect

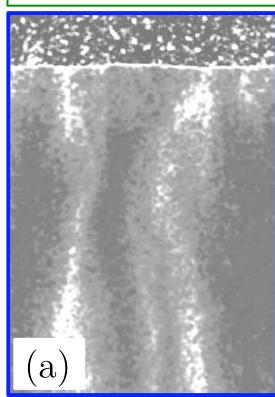


Theory: linear scaling $Sh = F Ra \sim Ra$ is expected (see review of Hewitt, 2020)

Porous media experiments: Sh \sim Ra $^{\alpha}$, α < 1 (Neufeld et al., Geophys. Res. Lett. 2010)

Hele-Shaw experiments: Sh $\sim \text{Ra}^{\alpha}$, $\alpha < 1$ (Backhaus et al., Phys. Rev. Lett. 2011)

Darcy simulations: Sh \sim Ra (Hidalgo et al., *Phys. Rev. Lett.* 2012)

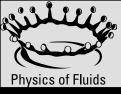






Differences arise due to effects not present in the Darcy model: consequences for porous media and Hele-Shaw

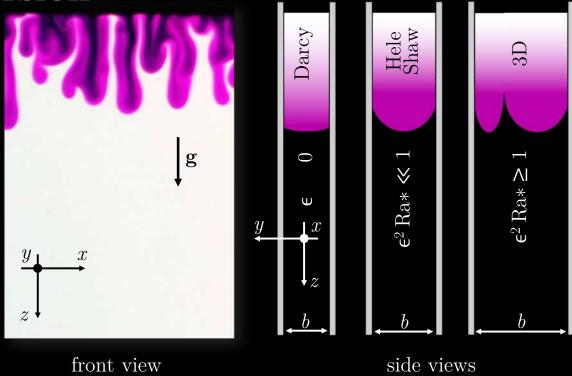
See De Paoli, Eur. Phys. J. E (2023) for a detailed discussion

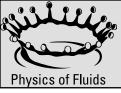


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Scalings of convection and finite-size effect



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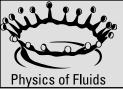






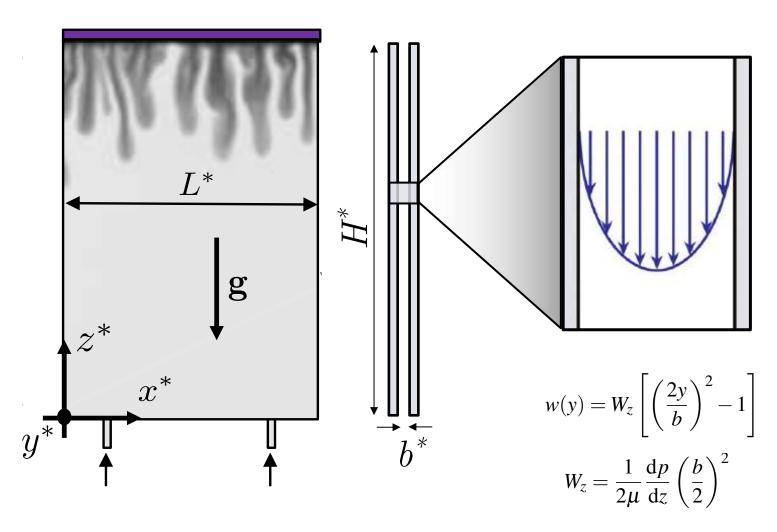
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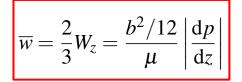
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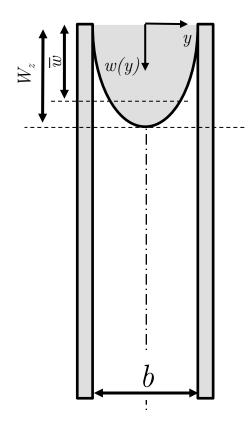


Experiments in Hele-Shaw cells

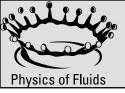






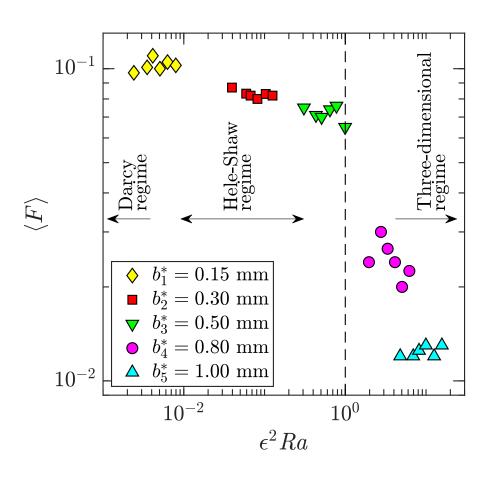


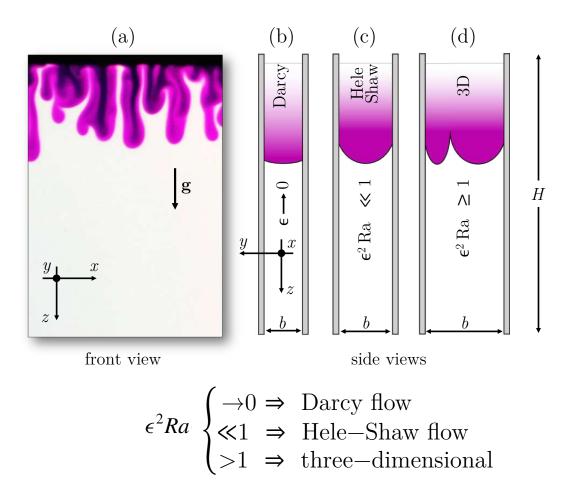
Alipour, De Paoli and Soldati, Exp. Fluids (2020) De Paoli, Alipour and Soldati, J. Fluid Mech. (2020)



Experiments in Hele-Shaw cells

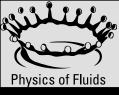






This model has been further developed in Letelier et al., J. Fluid Mech. (2023) Ulloa & Letelier, J. Fluid Mech. (2022)

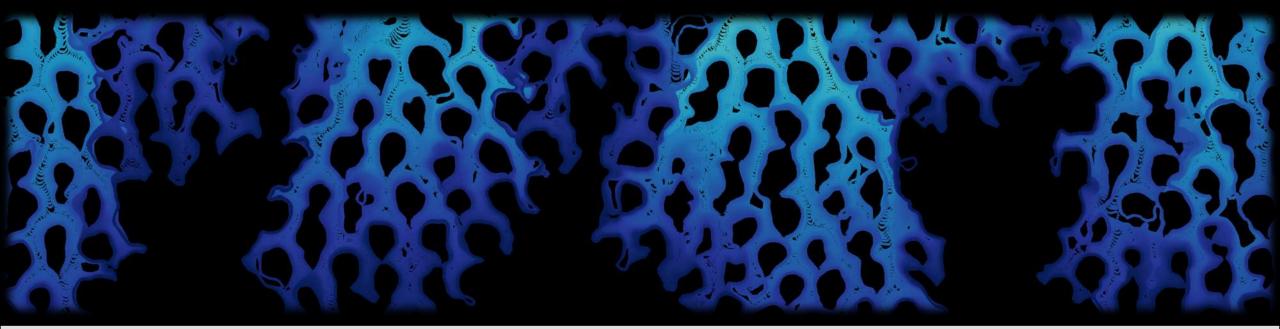
De Paoli, Alipour & Soldati, J. Fluid Mech. (2020)

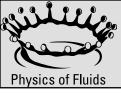


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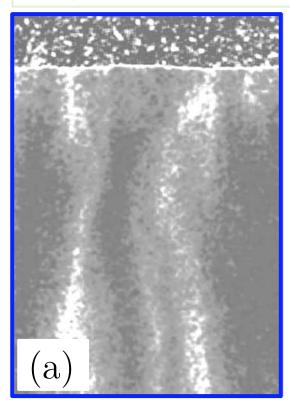


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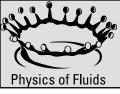






Differences arise due to effects not present in the Darcy model: consequences for **porous media** and **Hele-Shaw**

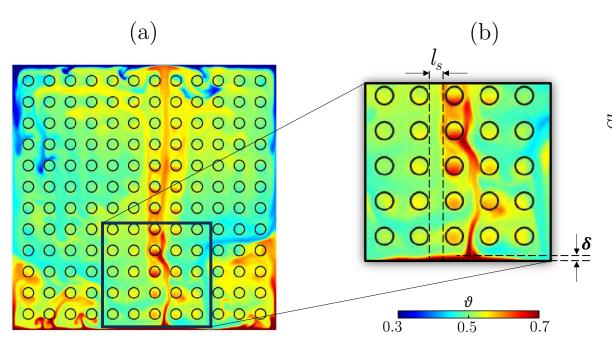
See De Paoli, Eur. Phys. J. E (2023) for a detailed discussion

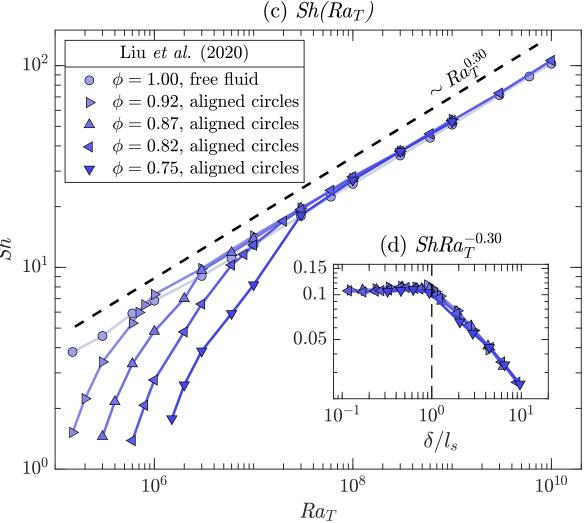


Pore-scale simulations



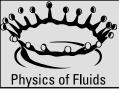
Additional non-Darcy effects: Relative size of flow structures and pores





Liu et al., *J. Fluid Mech.* (2020)

De Paoli, *Eur. Phys. J. E* (2023)



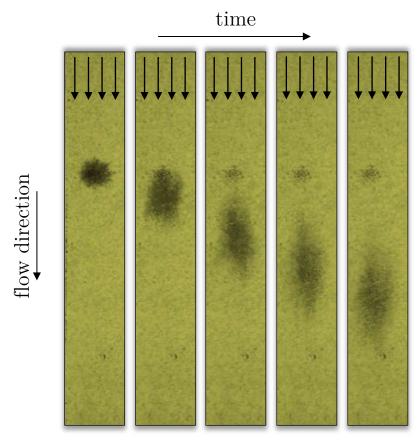
Influence of dispersion

columnar flow



Mechanism of dispersion

Patch of dye in a uniform flow through a porous medium



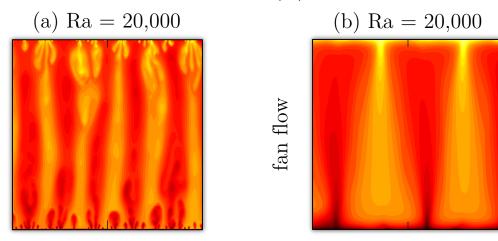
Woods, Flows in porous rocks (2015)

Darcy formulation of dispersion

$$\phi \frac{\partial C}{\partial t} + \nabla \cdot (\mathbf{u}C - \phi D \nabla C) = 0$$

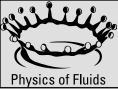
Fickian formulation for dispersion

$$\mathbf{D} = D\mathbf{I} + (\alpha_L - \alpha_T) \frac{\mathbf{u}\mathbf{u}}{|\mathbf{u}|} + \alpha_T \mathbf{u}\mathbf{I},$$



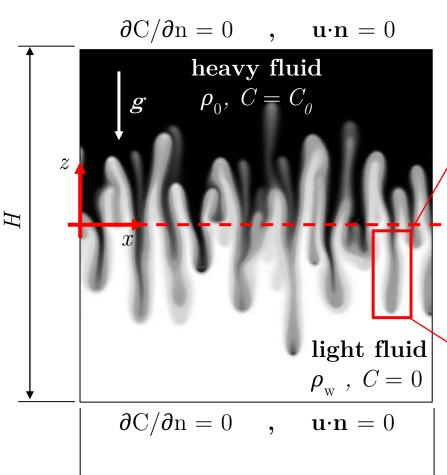
Liang et al., Geophys. Res. Lett. (2018) Chang et al., Phys. Rev. Fluids (2018)

These models required validation: Experiments and simulations in porous media

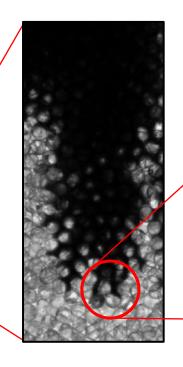


Flow configuration

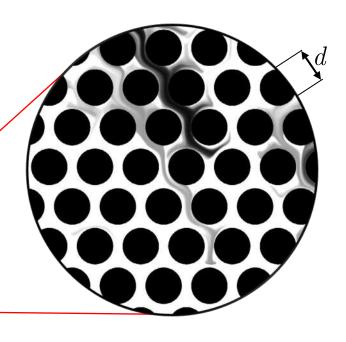




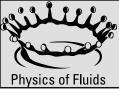
experiments



simulations

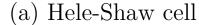


- High Schmidt number
- Porosity matched $\phi = 0.37$
- Solid impermeable to solute
- Linear dependency $\rho(C)$



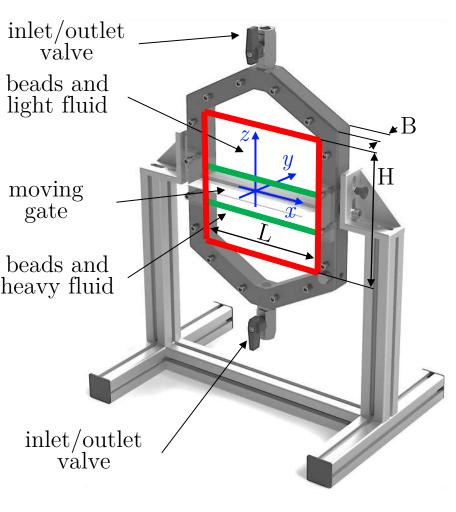
Experimental setup

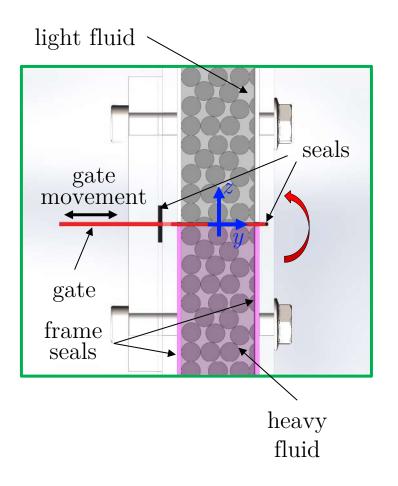


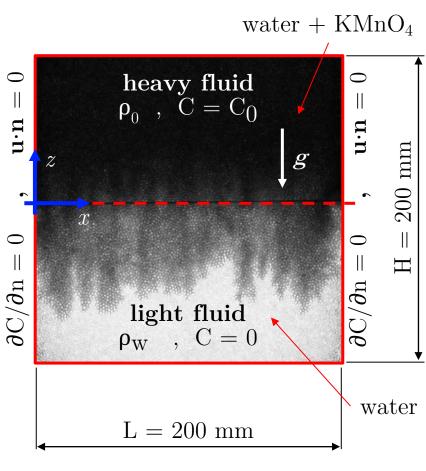


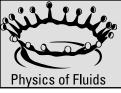
(b) gate (side view)

(c) measurement region



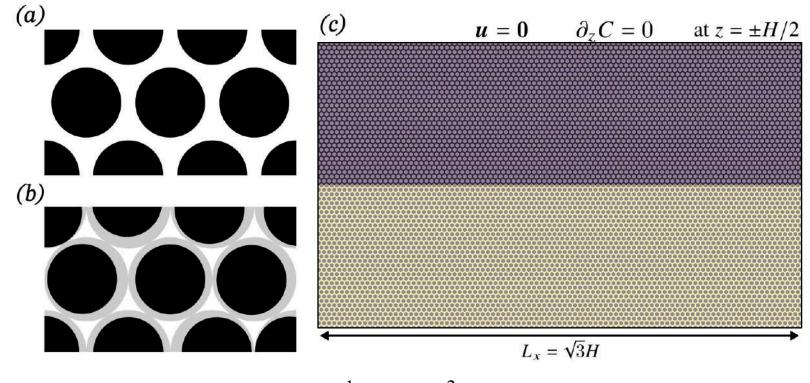






Numerical method





$$\partial_t \boldsymbol{u} + (\boldsymbol{u} \cdot \nabla) \boldsymbol{u} = -\rho_0^{-1} \nabla p + \nu \nabla^2 \boldsymbol{u} - g\beta C \hat{\boldsymbol{z}},$$

$$\partial_t C + (\boldsymbol{u} \cdot \boldsymbol{\nabla})C = D \nabla^2 C,$$

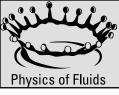
$$\rho = \rho_0 \left[1 + \frac{\Delta \rho}{\rho_0 C_0} (C - C_0) \right]$$

Finite difference (AFiD, open source)

Immersed
Boundaries Method

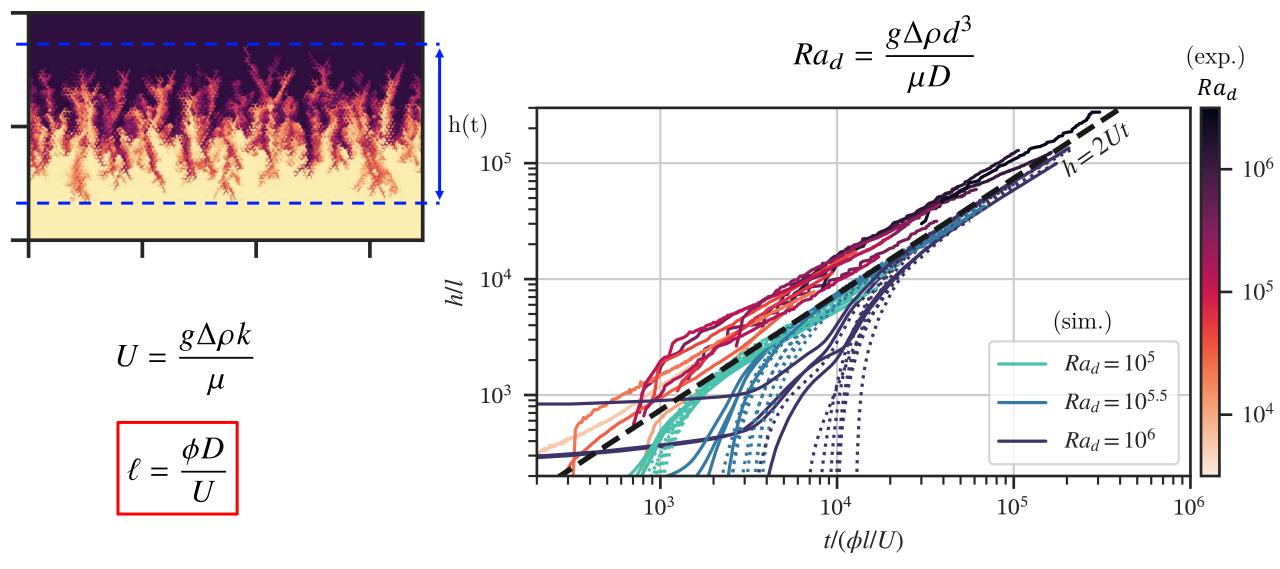
Resolution:

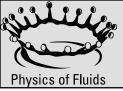
- velocity: ≥ 32 points
 per diameter
- conc. $: \ge 128$ points per diameter



Mixing length

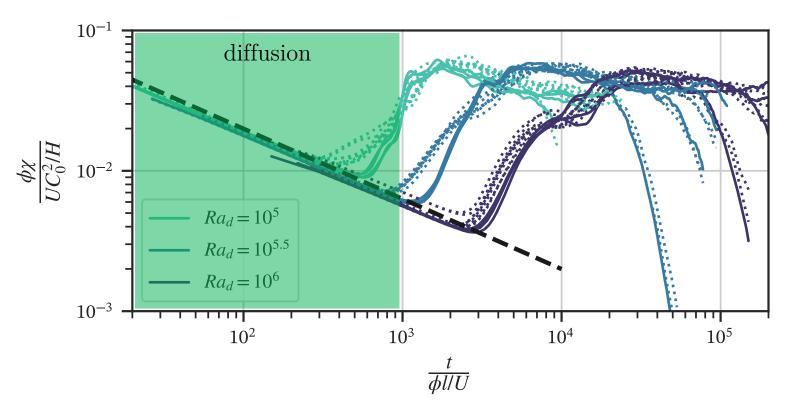








$$\chi = D\langle |\nabla C|^2 \rangle_f = \frac{D}{V_f} \int_{V_f} |\nabla C|^2 \ dV$$

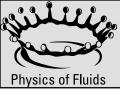


Can we model this mixing/dissolution process?

Diffusion:

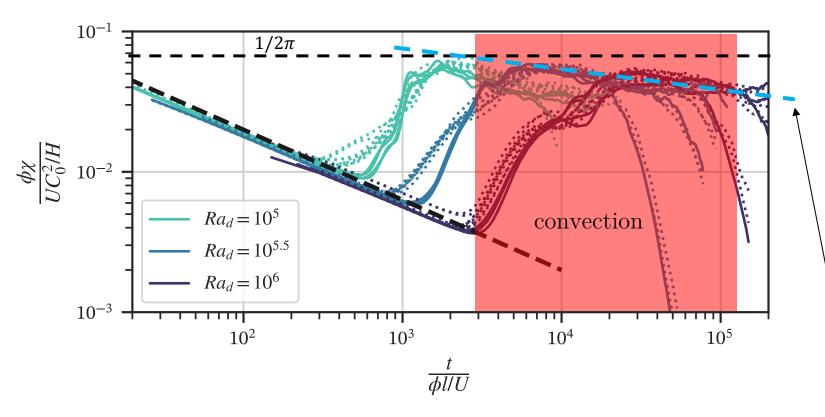
$$C = C_0 + \frac{\Delta C}{2} \operatorname{erf}\left(\frac{z}{\sqrt{2\kappa t}}\right)$$
$$\partial_z C = \frac{\Delta C}{2\sqrt{\pi \kappa t}} \exp\left(-\frac{z^2}{2\kappa t}\right)$$

$$\chi = \kappa \langle |\nabla C|^2 \rangle = \frac{\kappa}{H} \int_{-\infty}^{\infty} |\partial_z C|^2 dz$$
$$= \sqrt{\frac{\kappa}{8\pi t}} \frac{(\Delta C)^2}{H}$$





$$\chi = D\langle |\nabla C|^2 \rangle_f = \frac{D}{V_f} \int_{V_f} |\nabla C|^2 \ dV$$

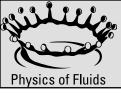


Convection

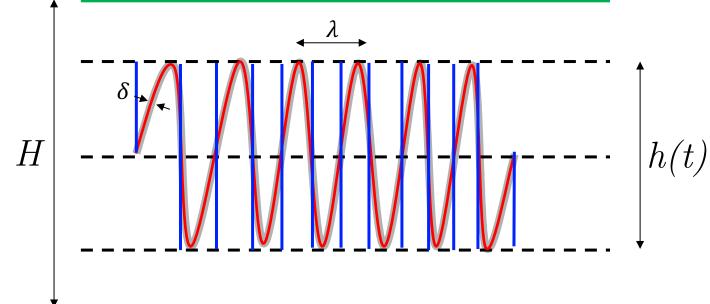
$$\chi = \kappa \langle |\nabla C|^2 \rangle = \kappa \frac{L_m}{H} \langle |\nabla C|^2 \rangle_{ML},$$
$$|\nabla C| \approx \frac{\Delta C}{2\sqrt{\pi \kappa t}}.$$
$$L_m \approx 2Ut,$$

$$\chi \approx \kappa \frac{2Ut}{H} \frac{(\Delta C)^2}{4\pi\kappa t} = \frac{1}{2\pi} \frac{U_d(\Delta C)^2}{H}.$$

 $1/2\pi$ is the maximum value of dissipation. Practically, χ decreases with time





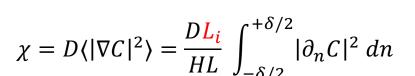


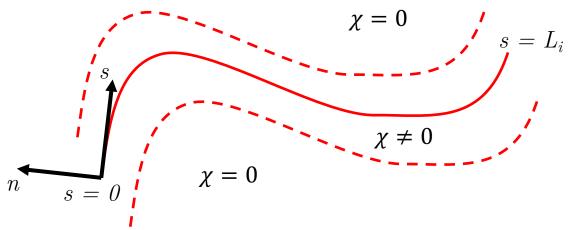
Assume:

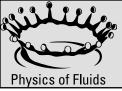
1) Interface grows as:

$$L_{i} = L + 2 N_{finger} h = L + 2 \frac{L}{\lambda} h$$

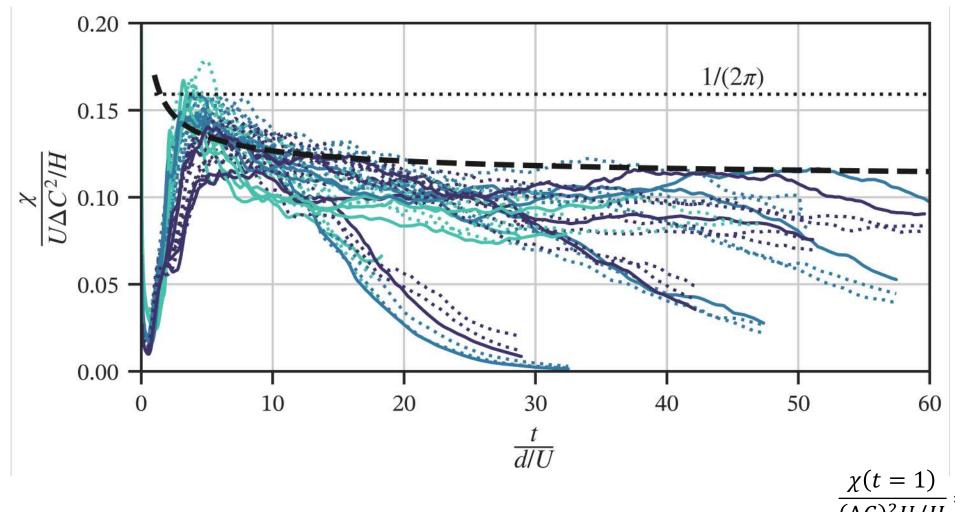
2) Gradient across the interface evolves according to the diffusive solution







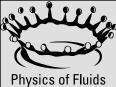




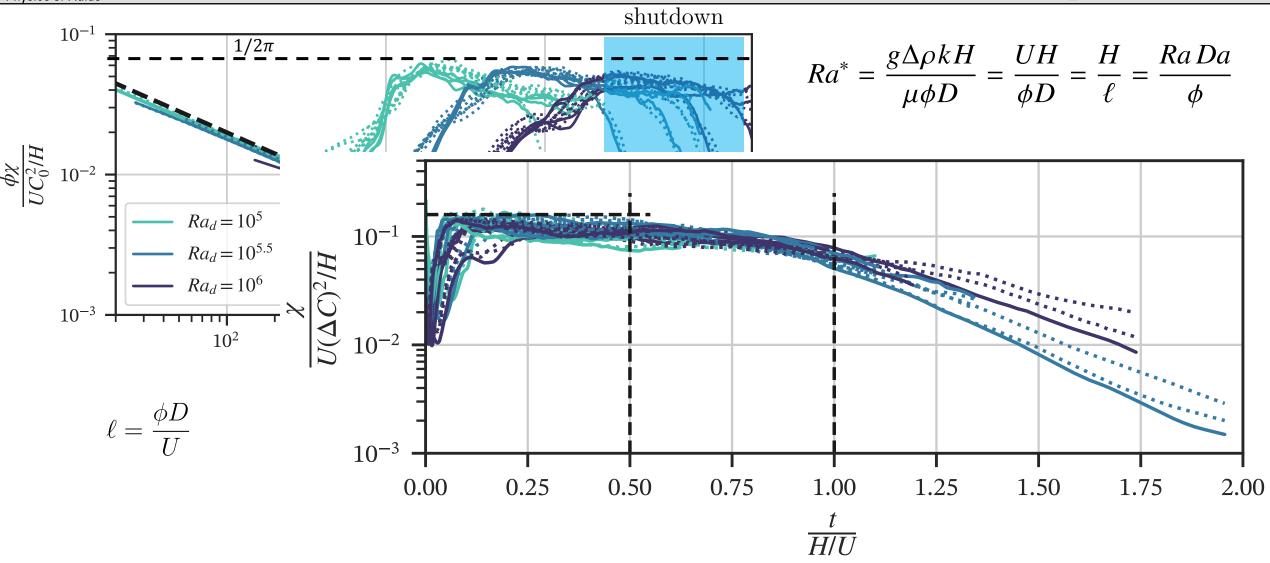
 $1/2\pi$ is the maximum value of dissipation.

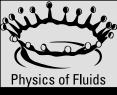
Model shown starting from t/(d/U) = 1. Time is also increased by d/U to account for initial condition.

$$\frac{\chi(t=1)}{(\Delta C)^2 U/H} = \frac{\beta}{\alpha \pi} \left(1 + \frac{\alpha}{4} \right) \approx \frac{1}{1.92\pi} \approx \frac{1}{2\pi}$$





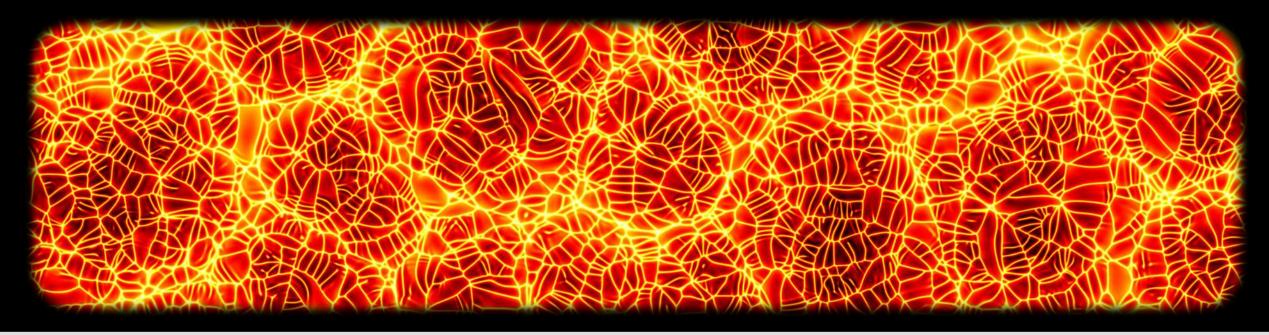


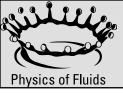


Presentation outline



- 1. Motivation
- 2. Reservoir-scale: multiphase gravity currents
- 3. Darcy-scale: simulations, experiments and finite-size effects
- 4. Pore-scale modelling and dispersion
- 5. Conclusions and outlook

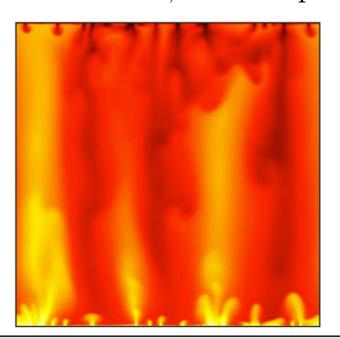


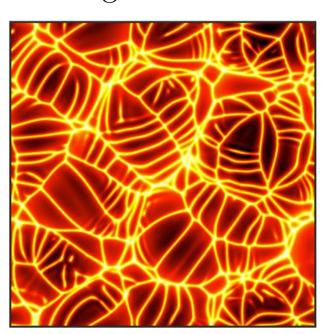


Conclusions and outlook



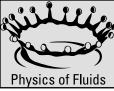
- 1. Convection in porous media is a **multiscale** and **multiphase** process
- 2. A combination of experiments, simulations and theory is required to model the flow dynamics
- 3. Recent developments in numerical and experimental capabilities enable measurements at unprecedented level of detail, but the parameters space is huge!





pore-scale

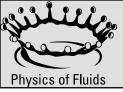




Conclusions and outlook









High-resolution images, movies and slides are available upon request to m.depaoli@utwente.nl